## The competitive effects of linking electricity markets across space

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## Motivation

- Regional virtual hubs for forward contracts is one of the proposed changes for a reformed EU market design
- Regional forward contracts settle against an average of short-term prices across multiple bidding zones
- In the Nordics, standard contracts settle against the common system price
- Purpose is to increase liquidity in the forward market relative to current market design


## Motivation

- This paper investigates the consequences for liquidity and efficiency of
- A regional forward market
- A regional short-term market (consumers pay average of local short-term prices)

Table 1: A taxonomy of market designs

|  | Local forward market | Regional forward market |
| :--- | :---: | :---: |
| Local short-term market | Default US market design | PJM, CAISO |
| Regional short-term market | Theory | NYISO, ISO-NE, Singapore, Italy |

## Modeling assumptions

- Two symmetric local markets (physically separate)
- One large consumer in each local market has inelastic demand $D$ for electricity
- One large generation owner in each local market produces electricity at marginal cost $c$
- A competitive fringe supplies residual demand in each local short-term market
- No uncertainty


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- A forward contract is a mechanism which
- increases efficiency in the short-term market
- enables consumers and producers to split the efficiency gains


## Timing of the game

- Each local producer commits to a forward price $f$
- Each large consumer purchases forward quantity $k$
- Each local producer supplies $q$ to the short-term market
- Solve the game backwards


## Short-term market

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Regional forward quantity half the pro-competitiye effect

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Forward premium smaller in regional forward market

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Equilibrium in a regional forward market

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k^{R}+\left[f^{R}-p^{R}\right] \frac{\partial k\left(f^{R}, f^{R}\right)}{\partial f}-P^{\prime}\left(q^{R}\right) q^{\prime}\left(k^{R}\right) \frac{k^{R}}{4} \frac{\partial k\left(f^{R}, f^{R}\right)}{\partial \tilde{f}}=0
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- A smaller forward premium
- A cross-price effect on the settlement price
- A larger own-price elasticity of forward demand


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- A cross-price effect on the settlement price
- A larger own-price elasticity of forward demand
- Regional forward market increases liquidity and market performance: $k^{R} \geq 2 k^{I}$


## Conclusions

- Novel mechanism for explaining forward contracting
- forward quantity increases efficiency in short-term market
- forward price splits value of efficiency gains between consumers and producers
- Market design affects gains from trade and their distribution
- A regional virtual hub increases liquidity and efficiency in the short-term market because of a substantial increase in own-price elasticity of demand
- Holds for any number of local markets and asymmetries
- Do not model costs of pooling local forward markets under uncertainty

